

## IN THE CLAIMS

1. (Currently Amended) ~~A method of inverting a 4x4 source matrix, the method~~ An article comprising a machine readable medium that stores data representing a predetermined function, the predetermined function comprising:

dividing the source matrix into four 2x2 sub-matrices  $A$ ,  $B$ ,  $C$  and  $D$ ;  
calculating a plurality of sub-matrix products from the sub-matrices;  
calculating a determinant of the source matrix  $dS$  to form a matrix determinant residue  $rd$  of the source matrix as  $rd=1/dS$ ;

forming a partial, inverse sub-matrix of each sub-matrix using one or more of the matrix products and a determinant of each sub-matrix; and

calculating an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$ , and  $iD$ , utilizing each partial, inverse sub-matrix and determinant residue  $rd$ , such that an inverse of the source matrix  $iS$  is formed.

2. (Currently Amended) The ~~method~~ article of claim 1, wherein dividing the source matrix  $S$  into the four 2x2 sub-matrices  $A$ ,  $B$ ,  $C$  and  $D$  is performed according to the following rule:

$$S = \begin{pmatrix} A & B \\ C & D \end{pmatrix}$$

to enable storage of each sub-matrix within a pair of SIMD registers.

3. (Currently Amended) The ~~article~~ method of claim 1, wherein calculating the plurality of sub-matrix products further comprises:

calculating an intermediate sub-matrix product for each sub-matrix by computing the following matrix equations:

$$\tilde{D}C = \text{adj}(D) \bullet C$$

$$\tilde{A}B = \text{adj}(A) \bullet B$$

wherein the  $\text{adj}$  function refers to an adjoint matrix operation and the dot symbol  $\bullet$  refers to a matrix multiplication operation; and

calculating a final sub-matrix product for each of the intermediate sub-matrix products by computing the following equations:

$$B\tilde{D}C = B \bullet \tilde{D}C$$

$$D\tilde{B}A = D \bullet \text{adj}(\tilde{A}B)$$

$$A\tilde{C}D = A \bullet \text{adj}(\tilde{D}C)$$

$$C\tilde{A}B = C \bullet \tilde{A}B.$$

4. (Currently Amended) The article method of claim 1, wherein calculating the matrix determinant residue further comprises:

computing a determinant of each sub-matrix  $dA$ ,  $dB$ ,  $dC$  and  $dD$ ;

calculating a trace value by computing a following equation:

$$t = \text{trace}(\tilde{A}B \bullet \tilde{D}C);$$

wherein a dot symbol  $\bullet$  refers to a matrix multiplication operation; and

calculating a determinant of the source matrix  $dS$  by computing a following equation:

$$dS = dA * dD + dB * dC - t$$

wherein the symbol  $*$  refers to a scalar multiplication operation.

5. (Currently Amended) The article method of claim 1, wherein forming partial-inverse sub-matrices further comprises:

performing matrix scaling of a determinant of each sub-matrix as  $D*dA$ ,  $C*dB$ ,  $B*dC$  and  $A*dD$ ; and

computing a partial inverse for each sub-matrix according to the following matrix scaling equations:

$$pA = A * dD - B\tilde{D}C$$

$$pB = C * dB - D\tilde{B}A$$

$$pC = B * dC - A\tilde{C}D$$

$$pD = D * dA - C\tilde{A}B,$$

wherein  $pA$ ,  $pB$ ,  $pC$ , and  $pD$  reference partial, inverse sub-matrices, and the symbol  $*$  refers to a matrix scaling by a scalar operation.

6. (Currently Amended) The article method of claim 1, wherein calculating an inverse of each sub-matrix further comprises:

calculating an adjoint value of each partial, inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$ , and  $pD$ , according to the following rules:

$$iA = \text{adj}(pA),$$

$$iB = \text{adj}(pB),$$

$$iC = \text{adj}(pC),$$

$$iD = \text{adj}(pD),$$

wherein the  $\text{adj}()$  function refers to the adjoint matrix operation;

calculating a final sub-matrix inverse value according to the following equations:

$$iA = iA * rd$$

$$iB = iB * rd$$

$$iC = iC * rd$$

$$iD = iD * rd,$$

wherein the symbol \* refers to a matrix scaling by a scalar operation; and  
forming the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$

7. (Currently Amended) An article comprising a machine readable medium that stores data representing a predetermined function, the predetermined function ~~A method~~ comprising:

dividing a source matrix into four 2x2 sub-matrices,  $A$ ,  $B$ ,  $C$  and  $D$ ;

calculating one or more intermediate sub-matrix products from one or more of the sub-matrices;

calculating a determinant of the source matrix to form a determinant residue  $rd$  utilizing the intermediate sub-matrix products;

scaling a determinant of each sub-matrix and the intermediate sub-matrix products using determinant residue  $rd$  to form final sub-matrix products;

forming a partial inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$  and  $pD$  for each sub-matrix using the scaled sub-matrix determinants and the final sub-matrix products; and

calculating an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$  and  $iD$ , utilizing each partial inverse sub-matrix to form an inverse source matrix  $iS$ .

8. (Currently Amended) The article ~~method~~ of claim 7, wherein calculating the matrix determinant residue further comprises:

computing a determinant of each sub-matrix  $dA$ ,  $dB$ ,  $dC$  and  $dD$ ;

calculating a trace value by computing a following equation:

$$t = \text{trace}(\tilde{A}B \bullet \tilde{D}C);$$

wherein a dot symbol  $\bullet$  refers to a matrix multiplication operation;

calculating a determinant of the source matrix  $dS$  by computing a following equation:

$$dS = dA * dD + dB * dC - t$$

wherein the symbol \* refers to a scalar multiplication operation; and

calculating the determinant residue  $rd$  according to the following rule:

$$rd = 1/dS.$$

9. (Currently Amended) The ~~article method~~ of claim 7, wherein scaling by the determinant residue further comprises:

multiplying each determinant by the determinant residue  $rd$  according to the following rules:

$$dA = dA * rd$$

$$dB = dB * rd$$

$$dC = dC * rd$$

$$dD = dD * rd;$$

multiplying each intermediate sub-matrix product  $\tilde{A}B$  and  $\tilde{D}C$  by the determinant residue  $rd$ , according to the following equations:

$$\tilde{D}C = \tilde{D}C * rd$$

$$\tilde{A}B = \tilde{A}B * rd; \text{ and}$$

calculating a final sub-matrix product for each of the intermediate matrix products by computing the following equations:

$$B\tilde{D}C = B \bullet \tilde{D}C$$

$$D\tilde{B}A = D \bullet \text{adj}(\tilde{A}B)$$

$$A\tilde{C}D = A \bullet \text{adj}(\tilde{D}C)$$

$$C\tilde{A}B = C \bullet \tilde{A}B.$$

10. (Currently Amended) The ~~article method~~ of claim 7, wherein calculating an inverse of each sub-matrix further comprises:

generating an adjoint of each partial, inverse sub-matrix by computing the following equations:

$$iA = \text{adj}(pA)$$

$$iB = \text{adj}(pB)$$

$$iC = \text{adj}(pC)$$

$$iD = \text{adj}(pD); \text{ and}$$

forming the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$

11. (Original) A computer readable storage medium including program instructions that direct a computer to function in a specified manner when executed by a processor, the program instructions comprising:

dividing the source matrix into four 2x2 sub-matrices A, B, C and D;

calculating a plurality of sub-matrix products from the sub-matrices;  
calculating a determinant of the source matrix  $dS$  to form a matrix determinant residue  $rd$  of the source matrix as  $rd=1/dS$ ;  
forming a partial, inverse sub-matrix of each sub-matrix using one or more of the matrix products and a determinant of each sub-matrix; and  
calculating an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$ , and  $iD$ , utilizing each partial, inverse sub-matrix and determinant residue  $rd$ , such that an inverse of the source matrix  $iS$  is formed.

12. (Original) The computer readable storage medium of claim 11, wherein dividing the source matrix  $S$  into the four  $2 \times 2$  sub-matrices  $A$ ,  $B$ ,  $C$  and  $D$  is performed according to the following rule:

$$S = \begin{pmatrix} A & B \\ C & D \end{pmatrix}$$

to enable storage of each sub-matrix within a pair of SIMD registers.

13. (Original) The computer readable storage medium of claim 11, wherein calculating the plurality of sub-matrix products further comprises:

calculating an intermediate sub-matrix product for each sub-matrix by computing the following matrix equations:

$$\tilde{D}C = \text{adj}(\tilde{D}) \bullet C$$

$$\tilde{A}B = \text{adj}(A) \bullet B$$

wherein the  $\text{adj}()$  function refers to an adjoint matrix operation and the dot symbol  $\bullet$  refers to a matrix multiplication operation; and

calculating a final sub-matrix product for each of the intermediate sub-matrix products by computing the following equations:

$$B\tilde{D}C = B \bullet \tilde{D}C$$

$$D\tilde{B}A = D \bullet \text{adj}(\tilde{A}B)$$

$$A\tilde{C}D = A \bullet \text{adj}(\tilde{D}C)$$

$$C\tilde{A}B = C \bullet \tilde{A}B.$$

14. (Original) The computer readable storage medium of claim 11, wherein calculating the matrix determinant residue further comprises:

computing a determinant of each sub-matrix  $dA$ ,  $dB$ ,  $dC$  and  $dD$ ;

calculating a trace value by computing a following equation:

$$t = \text{trace}(\tilde{A}B \bullet \tilde{D}C);$$

wherein a dot symbol  $\bullet$  refers to a matrix multiplication operation; and  
calculating a determinant of the source matrix  $dS$  by computing a following equation:

$$dS = dA * dD + dB * dC - t$$

wherein the symbol  $*$  refers to a scalar multiplication operation.

15. (Original) The computer readable storage medium of claim 11, wherein forming partial-inverse sub-matrices further comprises:

performing matrix scaling of a determinant of each sub-matrix as  $D*dA$ ,  $C*dB$ ,  $B*dC$  and  $A*dD$ ; and

computing a partial inverse for each sub-matrix according to the following matrix scaling equations:

$$pA = A * dD - \tilde{B}DC$$

$$pB = C * dB - \tilde{D}BA$$

$$pC = B * dC - \tilde{A}CD$$

$$pD = D * dA - \tilde{C}AB,$$

wherein  $pA$ ,  $pB$ ,  $pC$ , and  $pD$  reference partial, inverse sub-matrices, and the symbol  $*$  refers to a matrix scaling by a scalar operation.

16. (Original) The computer readable storage medium of claim 11, wherein calculating an inverse of each sub-matrix further comprises:

calculating an adjoint value of each partial, inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$ , and  $pD$ , according to the following rules:

$$iA = \text{adj}(pA),$$

$$iB = \text{adj}(pB),$$

$$iC = \text{adj}(pC),$$

$$iD = \text{adj}(pD),$$

wherein the  $\text{adj}()$  function refers to the adjoint matrix operation;

calculating a final sub-matrix inverse value according to the following equations:

$$iA = iA * rd$$

$$iB = iB * rd$$

$$iC = iC * rd$$

$$iD = iD * rd,$$

wherein the symbol  $*$  refers to a matrix scaling by a scalar operation; and

forming the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$

17. (Original) The computer readable storage medium including program instructions that direct a computer to function in a specified manner when executed by a processor, the program instructions comprising:

dividing a source matrix into four 2x2 sub-matrices,  $A$ ,  $B$ ,  $C$  and  $D$ ;

calculating one or more intermediate sub-matrix products from one or more of the sub-matrices;

calculating a determinant of the source matrix  $dS$  to form a determinant residue  $rd$  of the source matrix utilizing the intermediate sub-matrix products and the sub-matrix determinants;

scaling a determinant of each sub-matrix and the intermediate sub-matrix products using determinant residue  $rd$  to form final sub-matrix products;

forming a partial inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$  and  $pD$  for each sub-matrix using the scaled sub-matrix determinants and the final sub-matrix products; and

calculating an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$  and  $iD$ , utilizing each partial inverse sub-matrix to form an inverse source matrix  $iS$ .

18. (Original) The computer readable storage medium of claim 17, wherein calculating the matrix determinant residue further comprises:

computing a determinant of each sub-matrix  $dA$ ,  $dB$ ,  $dC$  and  $dD$ ;

calculating a trace value by computing a following equation:

$$t = \text{trace}(\tilde{A}B \bullet \tilde{D}C);$$

wherein a dot symbol  $\bullet$  refers to a matrix multiplication operation;

calculating a determinant of the source matrix  $dS$  by computing a following equation:

$$dS = dA * dD + dB * dC - t$$

wherein the symbol  $*$  refers to a scalar multiplication operation; and

calculating the determinant residue  $rd$  according to the following rule:

$$rd = 1/dS.$$

19. (Original) The computer readable storage medium of claim 17, wherein scaling by the determinant residue further comprises:

multiplying each determinant by the determinant residue  $rd$  according to the following rules:

$$dA = dA * rd$$

$$dB = dB * rd$$

$$dC = dC * rd$$

$$dD = dD * rd;$$

multiplying each intermediate sub-matrix product by the determinant residue  $rd$ , according to the following equations:

$$\tilde{D}C = \tilde{D}C * rd$$

$$\tilde{A}B = \tilde{A}B * rd; \text{ and}$$

calculating a final sub-matrix product for each of the intermediate matrix products by computing the following equations:

$$B\tilde{D}C = B \bullet \tilde{D}C$$

$$D\tilde{B}A = D \bullet \text{adj}(\tilde{A}B)$$

$$A\tilde{C}D = A \bullet \text{adj}(\tilde{D}C)$$

$$C\tilde{A}B = C \bullet \tilde{A}B.$$

20. (Original) The computer readable storage medium of claim 17, wherein calculating an inverse of each sub-matrix further comprises:

generating an adjoint of each partial, inverse sub-matrix by computing the following equations:

$$iA = \text{adj}(pA)$$

$$iB = \text{adj}(pB)$$

$$iC = \text{adj}(pC)$$

$$iD = \text{adj}(pD); \text{ and}$$

forming the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$



21. (Currently Amended) An apparatus, comprising:  
 a processor having circuitry to execute instructions;  
 a plurality of SIMD data storage devices coupled to the processor, the SIMD data storage registers to store pairs of floating point vectors during matrix calculation;  
 a storage device coupled to the processor, having sequences of instructions stored therein, which when executed by the processor cause the processor to:  
     divide the source matrix into four 2x2 sub-matrices  $A$ ,  $B$ ,  $C$  and  $D$ ;  
     calculate a plurality of sub-matrix products from the sub-matrices;  
     calculate a determinant of the source matrix  $dS$  to form a determinant residue  $rd$  of the source matrix as  $rd=1/dS$ ;  
     form a partial, inverse sub-matrix of each sub-matrix using one or more of the matrix products and the determinant of each sub-matrix; and  
     calculate an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$ , and  $iD$ , utilizing each partial, inverse sub-matrix and determinant residue  $rd$ , such that an inverse of the source matrix  $iS$  is formed.

22. (Original) The apparatus of claim 21, wherein the instruction to calculate the plurality of sub-matrix products further causes the processor to:

    calculate an intermediate sub-matrix product for each sub-matrix by computing the following matrix equations:

$$\tilde{D}C = \text{adj}(\tilde{D}) \bullet C$$

$$\tilde{A}B = \text{adj}(A) \bullet B$$

    wherein the  $\text{adj}()$  function refers to an adjoint matrix operation and the dot symbol  $\bullet$  refers to a matrix multiplication operation; and

    calculate a final sub-matrix product for each of the intermediate sub-matrix products by computing the following equations:

$$B\tilde{D}C = B \bullet \tilde{D}C$$

$$D\tilde{B}A = D \bullet \text{adj}(\tilde{A}B)$$

$$A\tilde{C}D = A \bullet \text{adj}(\tilde{D}C)$$

$$C\tilde{A}B = C \bullet \tilde{A}B.$$

23. (Original) The apparatus of claim 21, wherein the instruction to calculate the matrix determinant residue further causes the processor to:

    compute a determinant of each sub-matrix  $dA$ ,  $dB$ ,  $dC$  and  $dD$ ;

calculate a trace value by computing a following equation:

$$t = \text{trace}(\tilde{A}B \bullet \tilde{D}C);$$

wherein a dot symbol  $\bullet$  refers to a matrix multiplication operation; and

calculate a determinant of the source matrix  $dS$  by computing a following equation:

$$dS = dA * dD + dB * dC - t$$

wherein the symbol  $*$  refers to a scalar multiplication operation.

24. (Original) The apparatus of claim 21, wherein the instruction to perform matrix scaling further causes the processor to:

perform matrix scaling of a determinant of each sub-matrix as  $D*dA$ ,  $C*dB$ ,  $B*dC$  and  $A*DdD$ ;

compute a partial inverse for each sub-matrix according to the following matrix scaling equations:

$$pA = A * dD - B\tilde{D}C$$

$$pB = C * dB - D\tilde{B}A$$

$$pC = B * dC - A\tilde{C}D$$

$$pD = D * dA - C\tilde{A}B,$$

wherein  $pA$ ,  $pB$ ,  $pC$ , and  $pD$  reference partial, inverse sub-matrices and the symbol  $*$  refers to a matrix scaling by a scalar operation.

25. (Original) The apparatus of claim 21, wherein the instruction to calculate an inverse of each sub-matrix further causes the processor to:

calculate an adjoint value of each partial, inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$ , and  $pD$ , according to the following rules:

$$iA = \text{adj}(pA),$$

$$iB = \text{adj}(pB),$$

$$iC = \text{adj}(pC),$$

$$iD = \text{adj}(pD),$$

wherein the  $\text{adj}()$  function refers to the adjoint matrix operation;

calculate a final sub-matrix inverse value according to the following equations:

$$iA = iA * rd$$

$$iB = iB * rd$$

$$iC = iC * rd$$

$$iD = iD * rd,$$

wherein the symbol \* refers to a matrix scaling by a scalar operation; and  
form the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$

26. (Currently Amended) An apparatus, comprising:  
a processor having circuitry to execute instructions;  
a plurality of SIMD data storage devices coupled to the processor, the SIMD data storage registers to pairs of floating point vectors during matrix calculation;  
a storage device coupled to the processor, having sequences of instructions stored therein, which when executed by the processor cause the processor to:  
divide a source matrix into four 2x2 sub-matrices,  $A$ ,  $B$ ,  $C$  and  $D$ ;  
calculate one or more intermediate sub-matrix products from each of the sub-matrices,  
calculate a source matrix  $dS$  to form a determinant residue  $rd$  utilizing the intermediate sub-matrix products,  
scale a determinant of each sub-matrix and the intermediate sub-matrix products using determinant residue  $rd$  to form final sub-matrix products,  
form a partial inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$  and  $pD$  for each sub-matrix using the scaled sub-matrix determinants and the final sub-matrix products, and  
calculate an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$  and  $iD$ , utilizing each partial inverse sub-matrix to form an inverse source matrix  $iS$ .

27. (Currently Amended) The ~~apparatus~~ system of claim 26, wherein the instruction to calculate the source matrix determinant residue further causes the processor to:  
compute a determinant of each sub-matrix  $dA$ ,  $dB$ ,  $dC$  and  $dD$ ;  
calculate a trace value by computing a following equation:

$$t = \text{trace} (\tilde{A}B \bullet \tilde{D}C)$$

wherein a dot symbol  $\bullet$  refers to a matrix multiplication operation;  
calculate a determinant of the source matrix  $dS$  by computing a following equation:

$$dS = dA * dD + dB * dC - t$$

wherein the symbol \* refers to a scalar multiplication operation; and

calculate the determinant residue  $rd$  according to the following rule:

$$rd = 1/dS.$$

28. (Currently Amended) The ~~system apparatus~~ of claim 26, wherein the instruction to scale by the determinant residue further causes the processor to:

multiply each determinant by the determinant residue  $rd$  according to the following rules:

$$dA = dA * rd$$

$$dB = dB * rd$$

$$dC = dC * rd$$

$$dD = dD * rd;$$

multiply each intermediate sub-matrix product  $\tilde{A}B$  and  $\tilde{D}C$  by the determinant residue  $rd$ , according to the following equations:

$$\tilde{D}C = \tilde{D}C * rd$$

$$\tilde{A}B = \tilde{A}B * rd; \text{ and}$$

calculate a final sub-matrix product for each of the intermediate matrix products by computing the following equations:

$$B\tilde{D}C = B \bullet \tilde{D}C$$

$$D\tilde{B}A = D \bullet \text{adj}(\tilde{A}B)$$

$$A\tilde{C}D = A \bullet \text{adj}(\tilde{D}C)$$

$$C\tilde{A}B = C \bullet \tilde{A}B.$$

29. (Currently Amended) The ~~system apparatus~~ of claim 26, wherein the instruction to calculate an inverse of each sub-matrix further causes the processor to:

generate an adjoint of each partial, inverse sub-matrix by computing the following equations:

$$iA = \text{adj}(pA)$$

$$iB = \text{adj}(pB)$$

$$iC = \text{adj}(pC)$$

$$iD = \text{adj}(pD); \text{ and}$$

form the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$

Please add the following new claims:

-- 30. (New) A method comprising:  
dividing a source matrix into four 2x2 sub-matrices A, B, C and D;  
storing each two element row of each 2x2 sub-matrix within a single instruction multiple data (SIMD) register;  
forming a partial, inverse sub-matrix of each sub-matrix using one or more of a plurality of sub-matrix products calculated from the sub-matrices and a determinant of each sub-matrix within one or more SIMD registers; and  
calculating an inverse of each sub-matrix  $iA$ ,  $iB$ ,  $iC$  and  $iD$ , utilizing each partial, inverse sub-matrix and a determinant residue  $rd$  calculated from the source matrix, such that an inverse of the source matrix  $iS$  is formed within the one or more SIMD registers.

31. (New) The method of claim 30, wherein forming the partial inverse sub-matrix further comprises:  
calculating the plurality of sub-matrix products from the sub-matrices; and  
calculating the determinant of the source matrix  $Ds$  to form the matrix determinant residue  $rd$  of the source matrix as  $rd=1/Ds$ .

32. (New) The method of claim 30, wherein dividing the source matrix  $S$  into the four 2x2 sub-matrices A, B, C and D is performed according to the following rule:

$$S = \begin{pmatrix} A & B \\ C & D \end{pmatrix}$$

to enable storage of each sub-matrix within a pair of SIMD registers.

33. (New) The method of claim 31, wherein calculating an inverse of each sub-matrix further comprises:

calculating an adjoint value of each partial, inverse sub-matrix  $pA$ ,  $pB$ ,  $pC$ , and  $pD$ ,  
according to the following rules:

$$iA = \text{adj}(pA),$$

$$iB = \text{adj}(pB),$$

$$iC = \text{adj}(pC),$$

$$iD = \text{adj}(pD),$$

wherein the  $\text{adj}()$  function refers to the adjoint matrix operation;

calculating a final sub-matrix inverse value according to the following equations:

$$iA = iA * rd$$

$$iB = iB * rd$$

$$iC = iC * rd$$

$$iD = iD * rd,$$

wherein the symbol \* refers to a matrix scaling by a scalar operation; and  
forming the inverse source matrix  $iS$  according to the following rule:

$$iS = \begin{pmatrix} iA & iB \\ iC & iD \end{pmatrix}.$$